## 2009

ECONOMICS
DEPARTMENT

OCTAVIAN JULA

## MICROECONOMICS SEMINAR - WORKING PAPERS OCTAVIAN JULA

## SOME MATHEMATICAL TOOLS USED IN MICROECONONOMICS

Variation index: $\quad I_{x}=\frac{X_{1}}{X_{0}} \cdot 100$
Relative variation: $\quad I_{x}=\frac{X_{1}}{X_{0}} \cdot 100-100=\frac{\Delta X}{X_{0}} \cdot 100$
Absolute variation: $\Delta X=X_{1}-X_{0}$
if $\quad \mathrm{X}_{1}>\mathrm{X}_{0}\left(\right.$ so $\left.\mathrm{I}_{\mathrm{X}}>1\right)=>$ increase
$\mathrm{X}_{1}=\mathrm{X}_{0}\left(\right.$ so $\left.\mathrm{I}_{\mathrm{X}}=1\right)=>$ constant
$\mathrm{X}_{1}<\mathrm{X}_{0}\left(\right.$ so $\left.\mathrm{I}_{\mathrm{X}}<1\right)$ ) ${ }^{\text {d decrease }}$

## Example:

The nominal salary of an employee was at the beginning of the year 500 euro. On 31st of august the salary was 550 euro.

So, $I_{S i}=\frac{550}{500}=1,1$
This can be expressed in 3 different ways, but with the same meaning

- The salary increased by 1,1 times (coefficient of variation)
- The salary increased at $\mathbf{1 1 0 \%}$ (variation index)
- The salary increased with $\mathbf{1 0 \%}$ (relative variation)

So:

- The salary increased with 50 euro (absolute variation)

1. Same absolute variation determines different relative variations, depending on if there is and increase or a decrease.
Example:
To the same absolute variation - let's say 250 units - will correspond an relative increase by $25 \%$ (for example, from 1000 to 1250 units), and a decrease by only $20 \%$ (for a reduction from 1250 to 1000 de units).

- Increase: $I_{C}=\frac{1250}{1000} 100-100=25 \%$
- Decrease: $\quad I_{S}=\frac{1000}{1250} 100-100=-20 \%$

2. Consequent relative variations will not be summed in order to get the final relative variation for a wider period of time. The final relative variation can be determined as product from variation coefficients from those successive periods:

$$
\begin{gathered}
I_{\Sigma}=\prod_{i} \\
I_{\Sigma}=\left(\prod I_{i}\right) * 100 \\
I_{\Sigma}=\left(\prod I_{i}\right) * 100-100
\end{gathered}
$$

## Example:

An increase with $20 \%$ is followed by an increase with $30 \%$ so the total growth will not be $50 \%(30 \%+50 \%)$, but $56 \%(1,2 * 1,3 * 100-100)$ because the second increase of $30 \%$ is calculated also at the initial increase.

- Absolute total increase: $(100 * 1,2) * 1,3=120 * 1,3=156$
- Relative total increase: $I_{C}=\frac{156}{100} 100-100=56 \%$

3. Other calculus relations:

Arithmetical average: $\bar{m}=\frac{\sum_{l}^{n} x_{i}}{n}$
Growth: $\quad p=\frac{x_{i}}{\sum x_{i}} 100$
Arithmetical average with growth: $\quad \bar{m}=\frac{\sum x_{i} p_{i}}{\sum p_{i}}$

## INTRODUCTION AND UNSOLVED "MISTERIES"

## SOLVE THE NEXT EXAMPLES:

1. Establish the relations between the increase and the decrease from the table below:

| A relative <br> increase with | Is correspondent <br> to a decrease with | A relative <br> increase with | Is correspondent <br> to a decrease with |
| :---: | :---: | :---: | :---: |
| $1 \%$ | $\%$ | $50 \%$ | $\%$ |


| $2 \%$ | $\%$ | $100 \%$ | $\%$ |
| :---: | :---: | :---: | :---: |
| $3 \%$ | $\%$ | $200 \%$ | $\%$ |
| $10 \%$ | $\%$ | $300 \%$ | $\%$ |
| $25 \%$ | $\%$ | $500 \%$ | $\%$ |
| $33,3 \%$ | $\%$ | $900 \%$ | $\%$ |

2. Establish the relations between the increase and the decrease from the table below:

| A relative <br> increase with | Is correspondent <br> to a decrease with | A relative <br> increase with | Is correspondent <br> to a decrease with |
| :---: | :---: | :---: | :---: |
| $1 \%$ | $\%$ | $20 \%$ | $\%$ |
| $2 \%$ | $\%$ | $25 \%$ | $\%$ |
| $3 \%$ | $\%$ | $50 \%$ | $\%$ |
| $10 \%$ | $\%$ | $100 \%$ | $\%$ |

3. The government decided to index the salaries as follows: from $1^{\text {st }}$ of January with $8 \%$ and from $1^{\text {st }}$ of October with $12 \%$. What was the total increase in that year?
4. The monthly inflation rate was $1 \%$ in January, $1 \%$ in February and $1 \%$ in March. What is the total increase in the first three months of the year?
5. A decrease of the production in a certain period by $10 \%$ is followed by a next decrease with $20 \%$. What is the total decrease of the production from the initial moment?
6. An increase with $60 \%$ is followed by a decrease with $40 \%$. What is the evolution of the production?
7. An increase with $20 \%$ is followed by a decrease with $20 \%$ what is the evolution that will result from these elements?
8. The evolution of a certain price was:

| $\mathrm{t}_{1}$ | $\mathrm{t}_{2}$ | $\mathrm{t}_{3}$ | $\mathrm{t}_{4}$ | $\mathrm{t}_{5}$ | $\mathrm{t}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $+10 \%$ | $-10 \%$ | $+10 \%$ | $+20 \%$ | $+15 \%$ | $-10 \%$ |

What is the result of this evolution?
9. Represent graphically the next figures:

| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Y}_{1}$ | 10 | 35 | 55 | 70 | 80 | 85 | 85 | 75 |
| $\mathrm{Y}_{2}$ | 80 | 70 | 60 | 50 | 40 | 30 | 20 | 10 |



10. Represent graphically the function: $y=6-2 x$. Establish the relation between those two variables.
11. Read the data from the next graph and interpret them:


| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y |  |  |  |  |  |  |  |  |

A) What will be the change for Y (absolute and relative value) in $X=4$ in respect with $X=3$ ?
B) What about $\mathrm{X}=5$ towards $\mathrm{X}=4$ ?
12. Explain from the next graph the data regarding the demands from a certain product coming from 2 households $\left(\mathrm{C}_{1}\right.$ and $\left.\mathrm{C}_{2}\right)$ and present them into a table:


|  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

*Find the total demand.
13. Find the weight of each in the final price of gasoline:

|  | $l e i$ | $\%$ |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: |
| Production cost | 1,05 |  |  |  |  |
| Profit | 0,21 |  |  |  |  |
| Road tax | 0,35 |  |  |  |  |
| Luxury tax | 1,31 |  |  |  |  |
| Special tax | 0,02 |  |  |  |  |
| VAT | 0,56 |  |  |  |  |
| Total |  |  |  |  | 100 |

## WEDNESDAY, OCTOBER 07, 2009

## ACTIVTY, NEEDS AND INTERESTS

## PROBLEMS TO BE DISCUSSED:

1. Analyze:
A)

B)

2. Reply at the questions:
a) Is working, economic activity, an objective necessity?
b) What kind of links can we establish between desires and interests? What is the case with desires and purposes?
c) What will determine need's multiplication and diversity?
3. In which way laziness can be considered as a source for technological improvement?
4. The needs will be expressed in the wish of having:
A) Objects
B) Services
C) Informations
D) social recognition
E) all of above
F) none of them
